Mechanics 1 Revision

Vector Notation

- Vector quantities have both magnitude and direction, as opposed to scalars which have only magnitude.
- $\underline{\mathbf{a}} = x\underline{\mathbf{i}} + y\underline{\mathbf{j}}$

•
$$|\mathbf{a}| = magnitude = \sqrt{x^2 + y^2}$$

•
$$\hat{\mathbf{a}} = unit \ vector = \frac{\mathbf{a}}{|\mathbf{a}|}$$

- $\mathbf{r}_{a} = \text{position vector notation}$
- $\underline{\mathbf{r}_{\mathbf{a} \text{ relative to } \mathbf{b}}}_{\boldsymbol{\theta} = \mathbf{t} \mathbf{a} \mathbf{n}^{-1} \left(\frac{y}{r}\right)} = \underline{\mathbf{r}_{\mathbf{a}}} \underline{\mathbf{r}_{\mathbf{b}}}$

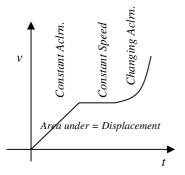
Kinematics

- For use with a constant acceleration
- v = u + at

•
$$s = \left(\frac{u+v}{2}\right)t$$

•
$$s = ut + \frac{1}{2}at^2$$

•
$$v^2 = u^2 + 2as$$



• Under gravity a = g = 9.8

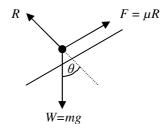
Statics

- Forces acting on a single point
- Forces must be in equilibrium
- In equilibrium $\sum F = 0$

Friction

- *Friction*, $F \leq \mu R$
- $F_{\text{max}} = \mu R$

Force Diagrams



Dynamics

- Using Newton; F = ma
- Now for coplanar forces $\sum F = ma$
- Connected Particles: *a* is the same on each body, resolve each body individually then add the equations to eliminate *T*

Momentum & Impulse

- P = mv in Ns
- Principle of Conservation of Momentum, $P_{before} = P_{after}$
- Impulse is ΔP
- Impulse is also = Ft
- \therefore *Ft* = *mv mu* in Ns

Moments

- Magnitude, Direction *and* point of application.
- Moment = $|F| \times d$ in Nm
- In equilibrium $\sum M = 0$
- Need a *sense* (clockwise or anti)
- A uniform rod's weight will act at its centre of mass.